

**CAMBRIDGE INTERNATIONAL EXAMINATIONS**

Cambridge International General Certificate of Secondary Education

## **MARK SCHEME for the May/June 2015 series**

### **0580 MATHEMATICS**

**0580/41**

Paper 4 (Paper 4 – Extended), maximum raw mark 130

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2015 series for most Cambridge IGCSE<sup>®</sup>, Cambridge International A and AS Level components and some Cambridge O Level components.

® IGCSE is the registered trademark of Cambridge International Examinations.

Page 2	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2015	0580	41

### Abbreviations

cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfw	not from wrong working
soi	seen or implied

Question	Answers	Mark	Part Marks
1	(a) (i) $\frac{13}{13+8+3} \times 12000$ with no subsequent errors	1	
	(ii) 4000	1	
	(b) $2 \times 6500 + 5 \times \text{their(a)(ii)} + (12000 - 6500 - \text{their(a)(ii)})$ or $(13 \times 2 + 8 \times 5 + 3 \times 1) \times 500$	2	<b>B1</b> for any two of $2 \times 6500$ , $5 \times \text{their(a)(ii)}$ , $(12000 - 6500 - \text{their(a)(ii)})$ seen or $13 \times 2 + 8 \times 5 + 3 \times 1$
	(c) 37 500	3	<b>M2</b> for $\frac{34500}{100-8} \times 100$ oe or <b>M1</b> for 34500 associated with $(100 - 8)\%$
	(d) $\frac{11}{26}$ cao	2	<b>M1</b> for any correct simplified version of $\frac{2750}{6500}$
(e) 89 500	1		
2	(a) 1.5 1.25 -0.75 0.5	4	<b>B1</b> for each
	(b) Fully correct curve	5	<b>B5</b> for correct curve over full domain or <b>B3 FT</b> for 11 or 12 points or <b>B2 FT</b> for 9 or 10 points or <b>B1 FT</b> for 7 or 8 points  <b>and</b> <b>B1</b> independent for one complete branch on each side of the $y$ -axis and <b>not touching</b> or crossing the $y$ -axis <b>SC4</b> for correct curve with branches joined

Page 3	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2015	0580	41

Question	Answers	Mark	Part Marks
	(c)	1	
		1	
		1	
	(d)	2	
	(e)	B1	
		2	<p>No daylight at <math>x = -1</math> Consider point of contact as midpoint between two vertices of daylight, the midpoint must be between <math>x = -1.1</math> and <math>-0.9</math></p> <p><b>dep on B1</b> or a close attempt at tangent at <math>x = -1</math></p> <p><b>or</b> <b>M1</b> for rise/run <b>also dep on</b> any tangent drawn or close attempt at tangent at any point. Must see correct or implied calculation from a drawn tangent</p>
3	(a) (i)	2	<p><b>SC1</b> for translation by <math>\begin{pmatrix} -1 \\ k \end{pmatrix}</math> or <math>\begin{pmatrix} k \\ 3 \end{pmatrix}</math> or 4 correct vertices plotted but not joined</p> <p><b>SC1</b> for correct size and orientation, wrong position or 4 correct vertices plotted but not joined</p> <p><b>B2</b> for 3 correct vertices plotted or if no / wrong plots allow <b>SC2</b> for 4 correct coordinates in column matrix or shown in working or <b>SC1</b> for any 3 correct coordinates or <b>M1</b> for <math>\begin{pmatrix} 1 &amp; 0 \\ 0 &amp; -1 \end{pmatrix} \begin{pmatrix} 2 &amp; 2 &amp; 3 &amp; 5 \\ 1 &amp; 2 &amp; 2 &amp; 1 \end{pmatrix}</math> oe</p>
	(ii)	2	
	(iii)	3	
	(b)	B1	
	enlargement	B1	not as column vector
	[centre] (1, 0)	B1	
	[scale factor] - 3	B1	
	(c)	2	<p><b>B1</b> for one correct row or column or <math>\begin{pmatrix} 0 &amp; 1 \\ -1 &amp; 0 \end{pmatrix}</math></p>

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2015	0580	41

Question	Answers	Mark	Part Marks
4	(a) 5	1	
	(b) $C \cap M$ oe	1	Allow e.g. $(B \cap C \cap M) \cup (C \cap M)$
	(c) 3	1	
	(d) (i) $\frac{8}{30}$ oe	1	0.267 or better
	(ii) $\frac{14}{30}$ oe	1	0.467 or better
	(e) $\frac{30}{272}$ oe	3	<b>M2</b> for $\frac{6}{17} \times \frac{5}{16}$ or <b>M1</b> for $\frac{6}{17}$ seen 0.110[2...] or better
5	(a) (i) 10.6 or 10.59...	2	<b>M1</b> for $\tan = \frac{55}{294}$ oe
	(ii) 175 or 174.9[...] to 175.[1...]	4	<b>M2</b> for [adj =] $\frac{55}{\tan 24.8}$ oe or <b>M1</b> for implicit version <b>and</b> <b>M1</b> dep on at least <b>M1</b> for 294 – <i>their</i> adj
	(b) (i) 4.9 or 4.89 to 4.9	4	<b>M3</b> for $\sqrt{4^2 + \left(\frac{1}{2}\sqrt{4.8^2 + 3^2}\right)^2}$ or <b>M2</b> for $\frac{1}{2}\sqrt{4.8^2 + 3^2}$ or <b>M1</b> for $\sqrt{4.8^2 + 3^2}$ or $2.4^2 + 1.5^2$
	(ii) 54.7 or 54.71 to 54.722	2	<b>M1</b> for $\sin = \frac{4}{\text{their } 4.9}$

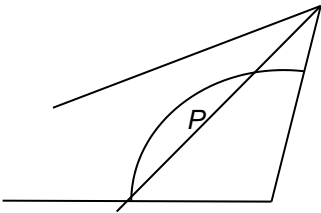
Page 5	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2015	0580	41

6	(a) (i)	$24 < t \leq 30$	1	
	(ii)	30.9 or 30.875 nfw	4	<p><b>M1</b> for midpoints <b>soi</b> (condone 1 error or omission) 5, 17, 27, 35, 50, 65 soi</p> <p><b>M1</b> for use of <math>\sum fx</math> with <math>x</math> in correct interval including both boundaries (condone 1 further error or omission) (50, 1530, 3645, 2975, 3500, 650) and <b>M1</b> (dep on 2<sup>nd</sup> <b>M1</b>) for <math>\sum fx \div 400</math></p>
	(b) (i)	[10 100] 235 320 390 [400]	2	<p><b>B1</b> for any two correct <b>SC1</b> for 235, <math>n, n + 70</math> <math>n &gt; 235</math></p>
	(ii)	Correct curve or polygon	3	<p><b>B1</b> for correct horizontal placement <b>B1FT</b> for correct vertical placement</p> <p><b>B1FT dep on at least B1</b> for reasonable increasing curve or polygon through their 6 points</p> <p>If zero scored <b>SC1</b> for 5 out of 6 points correctly plotted</p>
	(c) (i)	27.5 to 29	1	
	(ii)	12 to 14	2	<b>B1</b> for 36 to 38 or 24 seen
	(iii)	18 to 20	2	<b>B1</b> for 60 seen or marked on grid
	(iv)	30 to 45	2	<b>B1</b> for 355 to 370 seen

Page 6	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2015	0580	41

7	(a) (i) 8.27 or 8.269... nfww	4	M2 for $7.6^2 + 8.4^2 - 2 \times 7.6 \times 8.4 \times \cos(62)$ oe or M1 for implicit form  A1 for $[PQ^2 = ]$ 68.3 to 68.5
	(ii) 28.2 or 28.18..	2	M1 for $0.5 \times 7.6 \times 8.4 \times \sin 62$ oe
	(b) 55.8 or 55.78 to 55.79 nfww	5	B1 for $[HGJ] = 81$  B1 for $[GHJ] = 61$  M2 for $[GJ = ] \frac{63}{\sin(\text{their } 81)} \times \sin(\text{their } 61)$ or M1 for implicit form After M0, SC1 for final answer of 68.1...
8	(a) $5x = 75$ or $5x + 48 = 123$  15	B2  B1	M1 for $x + (x + 12) + 3(x + 12) = 123$ oe
	(b) 6, 7	3	B2 for answer of 6 or 7 OR M1 for $t < 8$ M1 for $t \geq \frac{37}{7}$ OR SC2 for final answer of 5, 6, 7 or 6, 7, 8 or SC1 for final answer of 5, 6, 7, 8
	(c) (i) 1.8 oe	3	M1 for $21 - x = 4(x + 3)$ or better B1 for $[\pm]5x = k$ or $kx = [\pm]9$
	(ii) $\sqrt{7^2 - 4 \times 3 \times (-5)}$ or better nfww  and  $\frac{-7 + \sqrt{q}}{2(3)}$ or $\frac{-7 - \sqrt{q}}{2(3)}$ oe  -2.91 and 0.57 final ans cao	B1    B1  B1B1	or for $\left(x + \frac{7}{6}\right)^2$  or for $-\frac{7}{6} \pm \sqrt{\frac{5}{3} + \left(\frac{7}{6}\right)^2}$  SC1 for 0.6 or 0.573... and -2.9 or -2.907 or -2.906... or -0.57 and 2.91 or 0.57 and -2.91 seen in working

Page 7	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2015	0580	41

9	(a) (i)	42	2	<b>B1</b> for $BAC = 90 - 48$
	(ii)	111	2	<b>B1</b> for 111 or 69 or $ACD = 27$ correctly placed on diagram or indicated
	(b) (i)	37.7 or 37.69 to 37.704 nfw	2	<b>M1</b> for $6\pi + 4\pi \pm 2\pi$ oe
	(ii)	12100, 12060, 12070, 12062.4 to 12065.6 nfw	5	<b>SC4</b> for answer with figs 121 or 1206 to 1207 <b>OR</b> <b>M2</b> for total area = $\frac{1}{2}\pi 6^2 + \frac{1}{2}\pi 4^2 - \frac{1}{2}\pi 2^2$ or $\frac{1}{2}\pi 60^2 + \frac{1}{2}\pi 40^2 - \frac{1}{2}\pi 20^2$ or <b>M1</b> for $\frac{1}{2}\pi 6^2$ or $\frac{1}{2}\pi 4^2$ or $\frac{1}{2}\pi 2^2$ or $\frac{1}{2}\pi 60^2$ or $\frac{1}{2}\pi 40^2$ or $\frac{1}{2}\pi 20^2$  <b>A1</b> for area = 75.39 to 75.41 or 7539 to 7541 <b>and</b> <b>M1 dep</b> for volume = <i>their</i> area $\times$ thickness
10	(a)	475 or 465 to 485	2	<b>B1</b> for 9.3 to 9.7 [cm] seen
	(b)	Correct perpendicular bisector with two pairs of intersecting arcs	2	<b>B1</b> for accurate with no/wrong arcs or <b>M1</b> for correct intersecting arcs
	(c)	Compass drawn arc centre <i>B</i> radius 5.8  Accurate angle bisector at <i>C</i> with correct intersecting arcs  	2	<b>M1</b> for compass drawn arc centre <i>B</i> or <b>B1</b> for 5.8 cm stated or used
		2	<b>B1</b> for accurate with no/wrong arcs or <b>M1</b> for correct intersecting arcs	
			1	cao

Page 8	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2015	0580	41

<p><b>11 (a)</b></p>	$\frac{At}{t+r}$ <p>final answer oe nfw</p>	<p><b>4</b></p>	<p><b>B1</b> for <math>t(A-x) = xr</math>  or <math>tA - tx = xr</math>  or <math>A = \frac{xr}{t} + x</math></p> <p><b>M1</b> for correctly completing multiplication by <math>t</math> (eliminating any bracket) and <math>x</math> terms isolated  <b>M1</b> for correct factorisation  <b>M1</b> dep for correct division</p>
<p><b>(b)</b></p>	<p>[a = ] 64</p> <p>[b = ] -8</p>	<p><b>3</b></p>	<p><b>B1</b> for <math>2b = -16</math> or <math>(x-8)^2</math></p> <p><b>B1</b> for <math>a = (their\ b)^2</math></p> <p>If <b>0</b> scored, <b>SC1</b> for <math>x^2 + 2bx + b^2</math> soi</p>
<p><b>(c)</b></p>	$\frac{13x+8}{(x-4)(3x-2)}$ <p>final answer nfw</p>	<p><b>3</b></p>	<p><b>B1</b> for <math>6(3x-2) - 5(x-4)</math> or better seen</p> <p><b>B1</b> for <math>(x-4)(3x-2)</math> oe seen as denom</p> <p>or <b>SC2</b> for final answer <math>\frac{13x-32}{(x-4)(3x-2)}</math></p>